

FACULTY OF ENGINEERING**B.E. 2/4 I-Semester (Main) Examination, November 2016****Subject : Mathematics – III (Common to All Except I.T. and ECE)****Time : 3 hours****Max. Marks : 75****Note: Answer all questions from Part-A and answer any FIVE questions from Part-B.****PART – A (25 Marks)**

- 1 Eliminate the arbitrary function to obtain a partial differential equation from $z = xy + f(x^2 - y^2)$. 3
- 2 Solve $p^2 x(1+y^2) = qy$. 2
- 3 Find the Fourier half range sine series of the function $f(x) = x+x^2, 0 < x < 1$. 3
- 4 Solve $3 \frac{\partial u}{\partial x} + 2 \frac{\partial u}{\partial y} = 0, u(x, 0) = 4 e^{-x}$. 2
- 5 If $P(A) = 0.4, P(B) = 0.6, P(A/B) = 0.5$ then find $P(B/A)$ and $P(A \cup B)$. 3
- 6 A continuous random variable X has the probability density function

$$f(x) = \begin{cases} a + bx, & 0 \leq x \leq 1 \\ 0 & \text{otherwise} \end{cases}$$
 If the mean of the distribution is $\frac{1}{3}$, find the values of a and b . 2
- 7 If X is a Poisson variate such that
 $P(X = 2) = 3P(X = 4) + 45P(X = 6)$, then find the mean of X . 3
- 8 Define χ^2 distribution and find its mean. 2
- 9 Write normal equations to fit a straight line $y = a + bx$. 3
- 10 Two random variables have the regression lines with equations $3x + 2y = 26$ and $6x + y = 31$. Find the mean values \bar{x} and \bar{y} . 2

PART – B (50 Marks)

- 11 a) Find the general solution of the partial differential equation
 $2xzp + 2yzq = z^2 - x^2 - y^2$. 5
- b) Find the complete integral of $(p^2 + q^2)x = pz$ by Charpit's method. 5

..2

12 Find the Fourier series of the function 10

$$f(x) = \begin{cases} 0 & \text{if } -\bar{\lambda}, x < 0 \\ x^2 & \text{if } 0 \leq x, \bar{\lambda} \end{cases}$$

and hence show that $\frac{f^2}{6} = 1 + \frac{1}{2^2} + \frac{1}{3^2} + \frac{1}{4^2} + \dots$

13 Solve the wave equation $\frac{\partial^2 u}{\partial t^2} = C^2 \frac{\partial^2 u}{\partial x^2}$, $0 < x < l$. $u(0, t) = u(l, t) = 0$,
 $u(x, 0) = x(l - x)$, $\frac{\partial u}{\partial t}(x, 0) = 0$. 10

14 Find the moment generating function of a random variable with pdf
 $f(x) = \frac{1}{c} e^{-\frac{x}{c}}$, $0 \leq x < \infty$, $c > 0$. Hence find its mean and standard deviation. 10

15 If X is a normal variate with mean 30 and S.D. 5, then find the probabilities that 10
 i) $26 \leq x \leq 40$ ii) $x \geq 45$ iii) $|x - 30| > 5$
 $(P(0 \leq z \leq 0.8) = 0.2881$; $P(0 \leq z \leq 2) = 0.4772$ $P(0 \leq z \leq 1) = 0.3413$).

16 a) Two independent samples of size 7 and 6 have the following values : 5

| | | | | | | | |
|----------|----|----|----|----|----|----|----|
| Sample A | 28 | 30 | 32 | 33 | 33 | 29 | 34 |
| Sample B | 29 | 30 | 30 | 24 | 27 | 29 | - |

Examine whether the samples have been drawn from normal populations having the same variance
 (Given that value of F at 5% level for (6, 5) d.f is 4.95 and for (5, 6) d.f is 4.39).

b) Find the mean of Gamma distribution. 5

17 a) Fit a parabola $y = a + bx + cx^2$ to the following data :

| | | | | | |
|---|---|-----|-----|-----|-----|
| X | 0 | 1 | 2 | 3 | 4 |
| y | 1 | 1.8 | 1.3 | 2.5 | 6.3 |

b) If θ is the angle between the two regression lines, then show that 5

$$\tan \theta = \frac{1-r^2}{r} \frac{\dagger_x \dagger_y}{\dagger_x^2 + \dagger_y^2}$$

Explain the significance when $r \pm 1$.

FACULTY OF ENGINEERING

B.E. 2/4 (ECE) I - Semester (Main) Examination, November / December 2016

Subject : Applied Mathematics

Time : 3 Hours

Max. Marks: 75

Note: Answer all questions from Part-A and answer any five questions from Part-B.**PART – A (25 Marks)**

- 1 Find a partial differential equation by eliminating the arbitrary function f from $z = f(\sin x + \cos y)$. (3)
- 2 Solve $p - q = z \sin(x+y)$. (2)
- 3 Determine $\lim_{z \rightarrow 0} \frac{\bar{z}}{z}$, if it exists. (3)
- 4 Evaluate $\int_C \frac{2z+7}{(z^2+1)(z-9)} dz$ where C is $|z| = \frac{1}{2}$. (2)
- 5 If $z = a$ is a simple pole of $f(z)$, prove that the residue of $f(z)$ at $z = a$ is $\lim_{z \rightarrow a} (z-a)f(z)$. (3)
- 6 Find the image of the region $|z| > 1$ under the transformation $w = \frac{i}{z-i}$. (2)
- 7 Explain Newton-Raphson method. (3)
- 8 Find the approximate value of $y(0.1)$ for $y' = 1 + y^2$, $y(0) = 1$ by Euler's method. (2)
- 9 Find the normal equations to fit a quadratic curve $y = a + bx + cx^2$ for the data. (3)

| | | | | | |
|---|---|-----|-----|-----|-----|
| x | 0 | 1 | 2 | 3 | 4 |
| y | 1 | 1.8 | 1.3 | 2.5 | 6.3 |

- 10 If one of the regression coefficients is greater than 1, show that the other regression coefficient is less than 1. (2)

PART – B (50 Marks)

- 11 (a) Solve $x(y^2 - z^2)p + y(z^2 - x^2)q - z(x^2 - y^2)r = 0$. (5)
- (b) Reduce the equation $z^2 = pqxy$ to the form $F(p, q) = 0$ and hence solve it. (5)
- 12 (a) Show that $u(x, y) = 2x + y^3 - 3x^2y$ is harmonic and find its conjugate harmonic function. (5)
- (b) State Cauchy's integral formula and use it to evaluate $\oint_C \frac{e^z}{z^2+1}$ where C is $|z - i| = 1$. (5)
- 13 (a) Find the Laurent series expansion of $f(z) = \frac{z}{(z-1)(z-3)}$ in the region $0 < |z - 1| < 2$. (5)
- (b) Evaluate $\int_0^\infty \frac{x^2}{(x^2+9)(x^2+4)^2} dx$. (5)

..2..

- 14 (a) Use Lagrange's interpolation formula to find $f(10)$ from the following data. (5)

| | | | | |
|------|----|----|----|----|
| x | 5 | 6 | 0 | 11 |
| f(x) | 12 | 13 | 14 | 16 |

- (b) Compute $f^{11}(1.5)$ by Newton's backward formula for the following data: (5)

| | | | | |
|------|------|------|------|------|
| x | 1 | 1.2 | 1.4 | 1.6 |
| f(x) | 1.01 | 1.18 | 1.33 | 1.56 |

- 15 (a) Fit a curve of the form $y = ae^{bx}$ to the following data: (5)

| | | | | | |
|---|------|------|------|------|------|
| x | 0.5 | 1.0 | 2.0 | 2.5 | 3.0 |
| y | 0.57 | 1.46 | 5.10 | 7.65 | 9.20 |

- (b) The ranks of 10 students in two subjects A and B are as follows: (5)

| | | | | | | | | | | |
|----|---|---|---|---|---|----|---|----|---|---|
| A: | 3 | 5 | 8 | 4 | 7 | 10 | 2 | 1 | 6 | 9 |
| B: | 6 | 4 | 9 | 8 | 1 | 2 | 3 | 10 | 5 | 7 |

Find the rank correlation coefficient.

- 16 (a) Solve $p^2 + q^2 = 1$ by Chapit's method. (5)

- (b) Evaluate $\int_0^{4+2i} \bar{z} dz$ along the curve $z = t^2 + it$. (5)

- 17 (a) Find the bilinear transformation which maps the points 0, -i, -1 of the z-plane into the points i, 1, 0 of the w-plane respectively. (5)

- (b) Find the regression line of x on y for the following data: (5)

| | | | | | | | | |
|---|---|---|---|---|---|---|---|---|
| x | 1 | 5 | 3 | 2 | 1 | 1 | 7 | 3 |
| y | 6 | 1 | 0 | 0 | 1 | 2 | 1 | 5 |

FACULTY OF INFORMATION

B.E. 2/4 (IT) I - Semester (Main) Examination, November / December 2016

Subject : Discrete Mathematics

Time : 3 Hours

Max. Marks: 75

Note: Answer all questions from Part-A and answer any five questions from Part-B.**PART-A (25 Marks)**

- 1 Translate the following English sentence into a logical expression:
"You cannot ride the roller coaster if you are under 4 feet tall unless you are older than 16 years old". [2]
- 2 Write the Converse, Inverse and Contra positive of the following implication:
"A positive integer is a prime only if it has no divisors other than 1 and itself". [3]
- 3 State Sum Rule. [2]
- 4 Seven women and nine men are on the faculty in the Mathematics department of a college. How many ways are there to select a committee of 5 members of the department if atleast one woman and atleast one man must be on the committee?[3]
- 5 Define Conditional Probability. [2]
- 6 State the Principle of Inclusion-Exclusion. [3]
- 7 How many relations are there on a set with 'n' elements? [2]
- 8 Define chromatic number of a graph. What is the chromatic number of K_n ? [3]
- 9 Define Strongly and Weakly connected graphs. [2]
- 10 What is the prefix form of the expression $[(x+2)^3] * [y - (3 + x)] - 5$. [3]

PART- B (50 Marks)

- 11 (a) Show that the following compound proposition is a tautology. [5]

$$[(p \vee q) \wedge (p \rightarrow r) \wedge (q \rightarrow r)] \rightarrow r$$
 (b) Show that $\neg(p \leftrightarrow q)$ and $\neg p \leftrightarrow q$ are logically equivalent. [5]
- 12 (a) Prove that $\sqrt{2}$ is irrational by giving a proof by contradiction. [5]
 (b) If 'n' is a positive integer then prove that $\sum_{k=0}^{\infty} C(n, k) = 2^n$. [5]
- 13 (a) Find the variance and standard deviation of the random variable 'X' whose value when two dice are rolled is $X[(i, j)] = i+j$, where 'i' is the number appearing on the first die and 'j' is the number appearing on the second die. [5]
 (b) Find the solution of the Recurrence Relation $a_n - 6a_{n-1} + 9a_{n-2} = n \cdot 3^n$. [5]
- 14 (a) If 'm' is a positive integer >1 then show that the relation $R = \{(a, b) / a \equiv b \pmod{m}\}$ is an equivalence relation on the set of integers. [5]
 (b) State and prove Euler's formula on planar graphs. [5]
- 15 (a) If 'G' is a connected planar simple graph with 'e' edges and 'v' vertices, show that $e = 3v - 6$. [5]
 (b) Explain Depth First Search algorithm to find a spanning tree with an example. [5]
- 16 (a) If 'X' is a random variable on a sample space 'S' then prove that $V(X) = E(X^2) - [E(X)]^2$. [5]
 (b) Find the coefficient of X^{10} in $(X^3 + X^4 + X^5 + \dots)^3$. [5]
- 17 (a) The bit strings for the sets $\{1,2,3,4,5\}$ & $\{1,3,5,7,9\}$ are 1111100000 & 1010101010 respectively. Use bit strings to find union and intersection of these sets. [5]
 (b) Prove that a tree with 'n' vertices has exactly (n-1) edges. [5]
