

**FACULTY OF ENGINEERING****B.E I – Year (Backlog) Examination, December, 2017****Subject : Engineering Physics****Time : 3 Hours****Max Marks : 75****Note: Answer all questions from Part – A & Any five questions from Part – B.****Part – A (25 MARKS)**

1. In a Newton's rings experiment the diameter of 10<sup>th</sup> ring changes from 1.40 to 1.27 cm when a drop of liquid is introduced between the lens and the glass plate. Calculate the refractive index of the liquid. [2]
2. Distinguish between Fresnel and Fraunhofer diffraction [3]
3. Mention few applications of optical fibres [2]
4. Derive Rayleigh Jeans Law and Wien's Law from Planck's Law [3]
5. What are Miller indices and explain with good example [3]
6. Discuss merits and demerits of classical free electron theory [3]
7. Write a note on frequency and temperature dependence of dielectric polarization [3]
8. Calculate the critical current for a wire of lead having a diameter of 1mm at 4.2K. Critical temperature for lead is 7.18K and critical field at 0K is  $6.5 \times 10^4$  A/m [2]
9. What are bulk and thin films? [2]
10. Write some properties of Nano - materials [2]

**PART – B**

11. a) Describe the construction of Nicol's prism and explain how it can be used as polarizer. [5]  
b) Discuss how hologram is recorded and how image is constructed from it [5]
- 12 a) What are fermions and obtain the Fermi – Dirac distribution function for fermions [5]  
b) Explain the working principle of an optical fiber [5]
13. a) Define the term Packing Fraction and find its value for SCC, BCC, FCC [4]  
b) Explain qualitatively Kronig Penny Model with discuss its conclusions [6]
- 14 a) What are different types of polarizations and derive an expression for ionic polarizability [5]  
b) Distinguish between soft and hard magnetic materials [5]
- 15 a) Explain sol-gel technique in preparing thin film [5]  
b) What are carbon Nano tubes and mention few applications [5]
16. a) Discuss Fraunhofer's diffraction at a single slit and explain intensity distribution [5]  
b) Apply the schroedinger's wave equation to a particle in an infinite square well potential and calculate its eigen values [5]
17. a) Distinguish between Type - 1 and Type - 2 superconductors [5]  
b) State and explain Hall Effect [5]

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## FACULTY OF ENGINEERING AND TECHNOLOGY

B.E/ B. Tech (Bridge Course) II-Semester Backlog Examination, December 2017

Subject: Mathematics

Time: 3 Hours

Max. Marks: 75

Note: Answer all questions of Part-A, &amp; Answer any FIVE questions from Part-B.

## PART-A

1. A coin is tossed thrice. Find the sample space [3]
2. Define discrete random variable [2]
3. Find the value of C of Rolle's Theorem for  $f(x) = x^2$  in  $[-1, 1]$ . [3]
4. Obtain the curvature of the curve  $y^2 = x$  at  $(1, 1)$ . [2]
5. Evaluate  $\int x e^x dx$  [3]
6. Find the area of the circle  $(x-1)^2 + y^2 = 4$  [2]
7. If  $\vec{F} = xy\hat{i} + yz\hat{j} + zx\hat{k}$ , find  $\nabla \cdot \vec{F}$  [3]
8. State Gauss's divergence theorem. [3]
9. Define Beta and Gamma functions [3]
10. Show that  $\text{erf}(x) + \text{erfc}(x) = 1$  [2]

## PART-B

11. (a) Find the median wage of the following distribution: [5]

Wages (in Rs.)	2000-3000	3000-4000	4000-5000	5000-6000	6000-7000
No. of Workers	3	5	20	10	5

- (b) If  $P(A) = \frac{1}{2}$ ,  $P(B) = \frac{1}{3}$ ,  $P(A \cap B) = \frac{1}{5}$ , then find (i)  $P(A \cap B)$  (ii)  $P(A \cap B^c)$  and (iii)  $P(A^c \cap B^c)$  [5]

12. (a) State and prove Cauchy's mean value theorem [5]

- (b) Find the Taylor series expansion of  $f(x) = \cos x$  about  $x = \frac{\pi}{4}$  [5]

13. (a) Evaluate  $\iint_R e^{2x+3y} dx dy$  over the triangle bounded by  $x=0$ ,  $y=0$  and  $x+y=1$  [5]

- (b) Evaluate  $\int_0^{\ln c} \int_0^{\ln b} \int_0^{\ln a} e^{x+y+z} dx dy dz$  [5]

14. (a) Find the directional derivative of the scalar function

$$f(x, y, z) = xy + yz + zx \text{ at } (1, 2, 0) \text{ in the direction of the vector } \hat{i} + 2\hat{j} + 2\hat{k}. [5]$$

- (b) If  $\vec{a}$  is a constant vector and  $\vec{r} = x\hat{i} + y\hat{j} + z\hat{k}$ , prove that  $\text{div}(\vec{a} \times \vec{r}) = 0$  [5]

15. (a) Prove that  $s(m, n) = \frac{\Gamma_m \Gamma_n}{\Gamma(m+n)}$  [5]

(b) Evaluate  $\int_0^1 \left(\ln \frac{1}{x}\right)^{n-1} dx, n > 0$  [5]

16. (a) State and prove multiplication theorem of probability [5]

(b) Find the envelope of the family  $(x-c)^2 + (y-c)^2 = c^2$ ,  $c$  is parameter [5]

17. Verify Green's theorem for  $\oint_C e^{-x} \sin y \, dx + e^{-x} \cos y \, dy$ , where  $C$  is the rectangle with vertices at  $(0,0), (f,0), (f, \frac{f}{2}), (0, \frac{f}{2})$ . [10]

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**FACULTY OF ENGINEERING**

B.E. I-Semester (Main &amp; Backlog) Examination, Dec, 2017

Subject: Engineering Mathematics-I

Time: 3 hours

Max. Marks: 70

Note: Answer all questions from Part-A and any Five Questions from part-B

**PART – A (20 Marks)**

1. Find the value of
- $\lambda$
- such that the rank of the matrix

$$\begin{bmatrix} 1 & 2 & 3 \\ 1 & 4 & 2 \\ 2 & 6 & \lambda \end{bmatrix} \text{ is } 2. \quad [2]$$

2. Find the sum and product of the eigen values of

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 3 & -1 \\ 0 & -1 & 3 \end{bmatrix}. \quad [2]$$

3. Test the convergence of the series
- $\sum_{n=1}^{\infty} \frac{4n^3 + 2}{7n^3 + 2n}$
- . [2]

4. Define the terms i) Absolute convergence and ii) Conditional convergence of a series with arbitrary terms. [2]

5. Find the radius of curvature of the curve
- $y = x^2 - 3x + 5$
- at
- $(1, 3)$
- . [2]

6. Find the envelope of the family of straight lines
- $y = mx + \frac{a}{m}$
- where 'm' is the parameter and 'a' is a constant. [2]

7. If
- $z = y + f(u)$
- ,
- $u = \frac{x}{y}$
- then show that
- $u \frac{\partial z}{\partial x} + \frac{\partial z}{\partial y} = 1$
- . [2]

8. If
- $u = x^2 + y^2$
- ,
- $v = 2xy$
- , find
- $\frac{\partial(u, v)}{\partial(x, y)}$
- . [2]

9. Show that
- $\vec{V} = 12x\hat{i} - 15y^2\hat{j} + \hat{k}$
- is irrotational. [2]

10. Find
- $\nabla f$
- at
- $(1, 2, -1)$
- if
- $f(x, y, z) = \log_e(x+y+z)$
- . [2]

**PART – B (50 Marks)**

11. a) Test for consistency and solve if consistent

$$x+2y+z=3; \quad 2x+3y+2z=5; \quad 3x-5y+5z=2; \quad 3x+9y-z=4.$$

b) Find the eigen values and eigen vectors of the matrix.

$$\begin{bmatrix} 2 & 1 & -1 \\ 1 & 1 & -2 \\ -1 & -2 & 1 \end{bmatrix}. \quad [5]$$

12. a) Test the convergence of the series.

$$\frac{x}{1.2} + \frac{x^2}{2.3} + \frac{x^3}{3.4} + \frac{x^4}{4.5} + \dots \text{to } \infty \quad [5]$$

b) Test the following series for conditional convergence.

$$\sum_{n=1}^{\infty} (-1)^{n-1} \frac{n}{n^2 + 1} \quad [5]$$

13. a) Verify Lagrange's Mean Value Theorem for  $f(x) = x(x-1)(x-2)$ ,  $x \in [0, 1/2]$ . [5]

b) Find the evolute of the parabola  $x^2 = 4ay$ . [5]

14. a) Expand  $f(x, y) = \tan^{-1}(xy)$  as a Taylor series about  $(1, 1)$  upto terms of second degree. [5]

b) Find  $\frac{\partial f}{\partial x}$  and  $\frac{\partial f}{\partial y}$  at  $(0, 0)$  given

$$f(x, y) = \begin{cases} \frac{xy}{x^2 + 2y^2}, & (x, y) \neq (0, 0) \\ 0, & (x, y) = (0, 0) \end{cases} \quad [5]$$

15. a) Find the directional derivative of  $w = xy^2 + yz^3$  at the point  $(2, -1, 1)$  in the direction of the normal to the surface  $x \log_e z - y^2 = -4$  at  $(-1, 2, 1)$ . [5]

b) If  $\vec{F} = (5xy - 6x^2)\hat{i} + (2y - 4x)\hat{j}$ , evaluate  $\int_C \vec{F} \cdot d\vec{R}$  along the curve C in the xy-plane given by  $y = x^3$ , from the point  $(1, 1)$  to  $(2, 8)$ . [5]

16. a) Using Cayley- Hamilton theorem find  $A^{-1}$

$$\text{if } A = \begin{bmatrix} 1 & 1 & 2 \\ 0 & -2 & 0 \\ 0 & 0 & 3 \end{bmatrix}. \quad [5]$$

b) Test the convergence of the series  $\sum_{n=1}^{\infty} \left(\frac{n}{n+1}\right)^n x^n, (x > 0)$ . [5]

17. a) Find the maxima and minima of  $f(x, y) = x^4 + y^4 - 2x^2 + 4xy - 2y^2$ . [5]

b) Prove that  $\nabla \cdot (\nabla \times \vec{A}) = 0$ , Where  $\vec{A}$  is a vector point function. [5]

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