

FACULTY OF ENGINEERING

B.E. 2/4 I - Semester (Backlog) Examination, November / December 2018

Subject : Mathematics – III (Common to All (Except I.T. & ECE))

Time : 3 Hours

Max. Marks: 75

Note: Answer all questions from Part-A & answer any five questions from Part-B.

PART – A (25 Marks)

- 1 Eliminate the arbitrary function of f to obtain a partial differential equation from
 $x^2 - y^2 + z^2 = f(xy)$ (3)

- 2 Find the complete integral of $px(1+y)=qy$. (2)

- 3 Find a_0 in the Fourier series expression of the (3)

$$\text{function } f(x) = \begin{cases} -x-f, & -f < x < 0 \\ x+f, & 0 < x < f \end{cases}$$

- 4 Solve $2u_x + u_t = 0$ where $u(0, t) = 5e^{-6t}$. (2)

- 5 Six boys and six girls sit in a row randomly. Find the probability that the six girls sit together. (3)

- 6 If the probability density function of a random variable 'X' is (2)

$$f(x) = \begin{cases} k x^{m-1} (1-x)^{n-1} & \text{for } 0 < x < 1 \\ 0 & , \text{ otherwise} \end{cases}$$

where $m > 0$ and $n > 0$ then find the value of k .

- 7 State any two applications of t – distribution. (3)

- 8 Find the mean of χ^2 - distribution. (2)

- 9 Fit a straight line of the form $y = a + bx$ to the following data. (3)

x	-1	3	5	7
y	1	7	10	13

- 10 Show that the geometric mean of regression coefficients is the coefficient of correlation. (2)

PART – B (50 Marks)

- 11 (a) Solve $(x^2 + y^2 + yz)=p+(x^2 + y^2 - xz)q = z(x+y)$. (5)

- (b) Find a complete integral of $p^2x + q^2y = z$ by using Charpit's method. (5)

..2..

12 Find the Fourier series of the function. (10)

$$f(x) = \begin{cases} x, & -f < x < 0 \\ f+x, & 0 < x < f \end{cases}. \text{ Hence deduce that}$$

$$1 - \frac{1}{3} + \frac{1}{5} - \frac{1}{7} + \dots = \frac{f}{4}.$$

13 Solve the Laplace equation $\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} = 0$ subject to the conditions
 $u(0, y) = u(a, y) = 0, u(x, 0) = x$ and $u(x, b) = 0$. (10)

14 A random variable X has the following probability distribution. (10)

x	1	2	3	4	5
P(x)	c	c	3c	c ² +c	6c ²

Then find the value of c. Also evaluate $P(X < 3)$, $P(1 < X < 4)$ and $P(X \geq 4)$

15 Let X be a random variable which follows normal distribution with mean 120 and the standard deviation 20. Evaluate

(i) $P(X \geq 140)$ (ii) $P(X \leq 80)$ and (iii) $P(100 \leq X \leq 115)$

(Given $P(0 \leq Z \leq 1) = 0.3413$, $P(0 \leq Z \leq 2) = 0.4772$. $P(0 \leq Z \leq \frac{1}{4}) = 0.08971$). (10)

16 (a) Using the method of least squares fit a curve of the form $y = ax^b$ to the following data. (5)

x	2	3	5	6
y	32	108	500	864

(b) Find the mean of two variables x and y and the correlation coefficient between x and y if the regression lines of y on x and x on y are $x + 6y = 6$, $2x + 3y = 9$ respectively. (5)

17 (a) Define Gamma distribution and find its variance. (5)

(b) Using the method of least squares, fit a parabola of the form $y = a + bx + cx^2$ to the following data (5)

x	-1	2	3	4	5
y	15	12	27	70	81

FACULTY OF ENGINEERING

B.E. 2/4 (ECE) I - Semester (Backlog) Examination, November / December 2018

Subject : Applied Mathematics

Time : 3 Hours

Max. Marks: 75

Note: Answer all questions from Part-A & any five questions from Part-B.

PART – A (25 Marks)

- 1 Form a partial differential equation by eliminating the arbitrary constants a and b from $z = ax^3 + by^3$ (2)
- 2 Find the complete integral of $p^2y(1 + x^2) = qx^2$ (3)
- 3 Show that $f(z) = \bar{z}$ is not analytic at any point. (2)
- 4 Evaluate $\int_C \frac{\sin z}{6z + f}$ where C is the circle $|z| = 1$ with positive orientation. (3)
- 5 Find the Taylor series of $f(z) = \frac{1-z}{z-2}$ around $z = 1$. (2)
- 6 Find the residue of $f(z) = \frac{3z+2}{z(z-1)(z-2)}$ at $z = 2$. (3)
- 7 Find the Lagrange interpolating polynomial which fits the following data. (2)

x	2	3
f(x)	8	11

- 8 If $y' = x + y - xy$, $y(0) = 2$ then evaluate $y(0.2)$ by using Euler's method. (Take $h = 0.1$) (2)
- 9 Show that the correlation coefficient is the geometric mean of the regression coefficients. (2)
- 10 Show that $t \leq r \leq 1$, r is the coefficient of correlation. (3)

PART – B (50 Marks)

- 11 (a) Find the complete integral of $xp + 3yq = 2(z - x^2 - q^2)$ by using Charpit's method. (5)
(b) Solve $p + q = x + y + z$ (5)
- 12 (a) Determine the analytic function $f(z) = u + iv$ if $u + v = e^x (\cos y + \sin y)$. (5)
(b) State and prove Cauchy's integral theorem. (5)
- 13 (a) Find the Laurent series of the function $f(z) = \frac{3}{2+z-z^2}$ in the regions (5)
(i) $1 < |z| < 2$ (ii) $|z| > 2$
(b) Evaluate $\int_0^{2\pi} \frac{\sin_n \theta}{3 + \cos_n \theta} d_n \theta$. (5)

..2..

- 14 (a) Find an approximate root of $x^3 + 4x - 7 = 0$ by using bisection method. (perform 4 iterations). (5)
- (b) Construct the forward difference table for the data: (5)

x	1	2	3	4
f(x)	1	18	71	178

Hence determine the corresponding interpolating polynomial.

- 15 (a) Find the regression line of Y on X from the following data: (5)

X	10	15	35	40	50
Y	100	90	110	80	120

- (b) Using the method of least squares, fit a curve $y = a + bx + cx^2$ to the following data. (5)

x	-1	1	2	3	5
y	7	5	1	-5	-23

- 16 (a) Evaluate $\int_C \bar{z} . dz$ where C is the line segment from $-1 - i$ to $3 + i$. (5)

- (b) Find the bilinear transformation which maps the points $z=1, i, -1$ onto $w = 0, 1, \infty$ respectively. (5)

- 17 (a) If $\frac{dy}{dx} = \frac{1}{x+y}$, $y(0)=1$ then evaluate $y(0.1)$ by using Runge-Kutta fourth order method. (5)

- (b) Find the rank correlation coefficient between X and Y from the following data which represents the marks of 5 students in two papers X and Y. (5)

X	10	12	15	14	19
Y	40	41	48	60	50

FACULTY OF ENGINEERING

B.E. 2/4 (IT) I-Semester (Backlog) Examination, November / December 2018

Subject : Discrete Mathematics

Time : 3 hours

Max. Marks : 75

Note: Answer all questions from Part-A. Answer any FIVE questions from Part-B.

PART – A (25 Marks)

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|---|---|
| 1 Show that the function $f : Z^+ \rightarrow Z^+$ defined by $f(x)$ is invertible. | 3 |
| 2 Find prime factorization of 7007. | 2 |
| 3 How many strings with seven or more characters can be formed from "EVERGREEN". | 2 |
| 4 State the generalized pigeonhole principle. | 2 |
| 5 In how many different ways can eight identical cookies be distributed among three distinct children if each child receives at least two cookies and no more than 4 cookies? | 3 |
| 6 State divide and conquer recurrence relation and give an example. | 2 |
| 7 Write short notes on representation of relations. | 3 |
| 8 Define Euler circuit and give an example. | 3 |
| 9 Define minimum spanning tree. | 2 |
| 10 Define graph isomorphism and give an example. | 3 |

PART – B (50 Marks)

- | | |
|---|----|
| 11 a) Show that $\sim(p \vee (\sim p \wedge q))$ and $\sim p \wedge q$ are logically equivalent by developing a series of logical equivalences. | 5 |
| b) What is the truth value of $f(x)$ if $p(x)$ is the statement " $x^2 > 10^4$ " and the universe of discourse consists of positive integers not exceeding 4? | 5 |
| 12 Using mathematical induction to prove formula of sums of geometric progression given? | 10 |

$$\sum_{j=0}^n ar^j = a + ar + ar^2 + \dots + ar^n = \frac{ar^{n+1} - a}{r - 1}$$

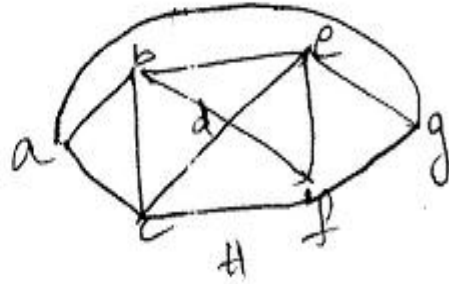
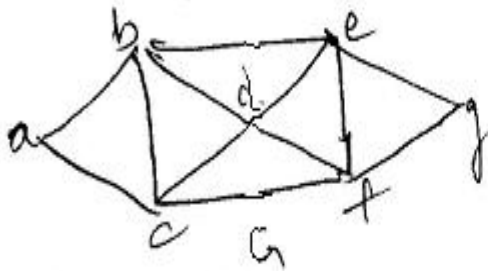
When $r \neq 1$, where n is non-negative integers.

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|--|----|
| 13 Find the solutions to the recurrence relation with initial conditions $a_0 = 2$, $a_1 = 5$
$a_n = 6a_{n-1} - 11a_{n-2}$. | 10 |
| 14 How many solutions to the $x_1 + x_2 + x_3 = 11$ have where x_1, x_2, x_3 are non negative integers with $x_1 \geq 3, x_2 \geq 4, x_3 \geq 6$? | 10 |

..2

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- 15 Draw Hasse diagram for poset $(\{1, 2, 3, 4, 6, 8, 12\}, 1)$. Find maximal, minimal, greatest and least element if any. 10
- 16 a) Define a planar graph. Draw a planar representation of K_4 . 4
 b) Find chromatic number of graph G and H 6



- 17 Explain Kruskal's algorithm to find minimal spanning tree with an example. 10

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FACULTY OF ENGINEERING**B.E. II – Semester (CBCS) (Supple.) Examination, Nov./Dec. 2018****Subject: Engineering Physics – II****Time: 3 Hours****Max. Marks: 70****Note: Answer all questions from Part A and any Five questions from Part B.****PART – A (10x2 = 20 Marks)**

- 1) Calculate the longest wavelength that can be analyzed by rock – salt crystal of spacing 2.5 \AA in the first order.
- 2) Define space lattice. How it is helpful to describe a crystal structure.
- 3) What are ferrites?
- 4) Define critical transition temperature and critical field for superconductors.
- 5) Calculate the Hall coefficient of a specimen whose electrical conductivity is 2.12 ohm/m and charge carrier mobility is $0.3 \text{ m}^2/\text{v}\cdot\text{sec}$
- 6) Discuss the important applications of ferro electric materials.
- 7) Distinguish between bulk, thin films and nano materials.
- 8) What are the applications of AFM?
- 9) Discuss the effect of surface to volume ratio in nano materials.
- 10) Mention the optical and magnetic properties of nano materials.

PART – B (50 Marks)

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|--|---|
| 11. a) Distinguish solid materials based on band theory of solids | 4 |
| b) Discuss the seven crystal systems in terms of lattice parametric consideration and type of Bravais lattice. | 6 |
| 12. a) What are magnetic domains? Explain the Hysteresis loop of ferromagnetic material. | 5 |
| b) Write a note on high temperature superconductors and their applications. | 5 |
| 13. a) How the P-N junction is formed? Explain V-I characteristic graph of forward and reverse bias phenomenon in PN junction diode. | 5 |
| b) How do you determine the dielectric constant by capacitance bridge method? | 5 |
| 14. a) Explain the principle and applications of X-ray Fluorescence. | 5 |
| b) Explain in detail about thermal evaporation technique to prepare thin films? | 5 |
| 15. a) What are nano materials? Why do they exhibit different properties? | 5 |
| b) Discuss the ball milling synthesis of nano materials. | 5 |
| 16. a) Discuss the free electron theory of metals. | 5 |
| b) Write a note on Type-I and Type-II superconductors? Explain their importance. | 5 |
| 17. a) Explain the phenomenon of ferro electricity and discuss how dielectric constant of Barium Titanate changes with temperature. | 5 |
| b) Describe the working of a thin film solar cell. | 5 |
