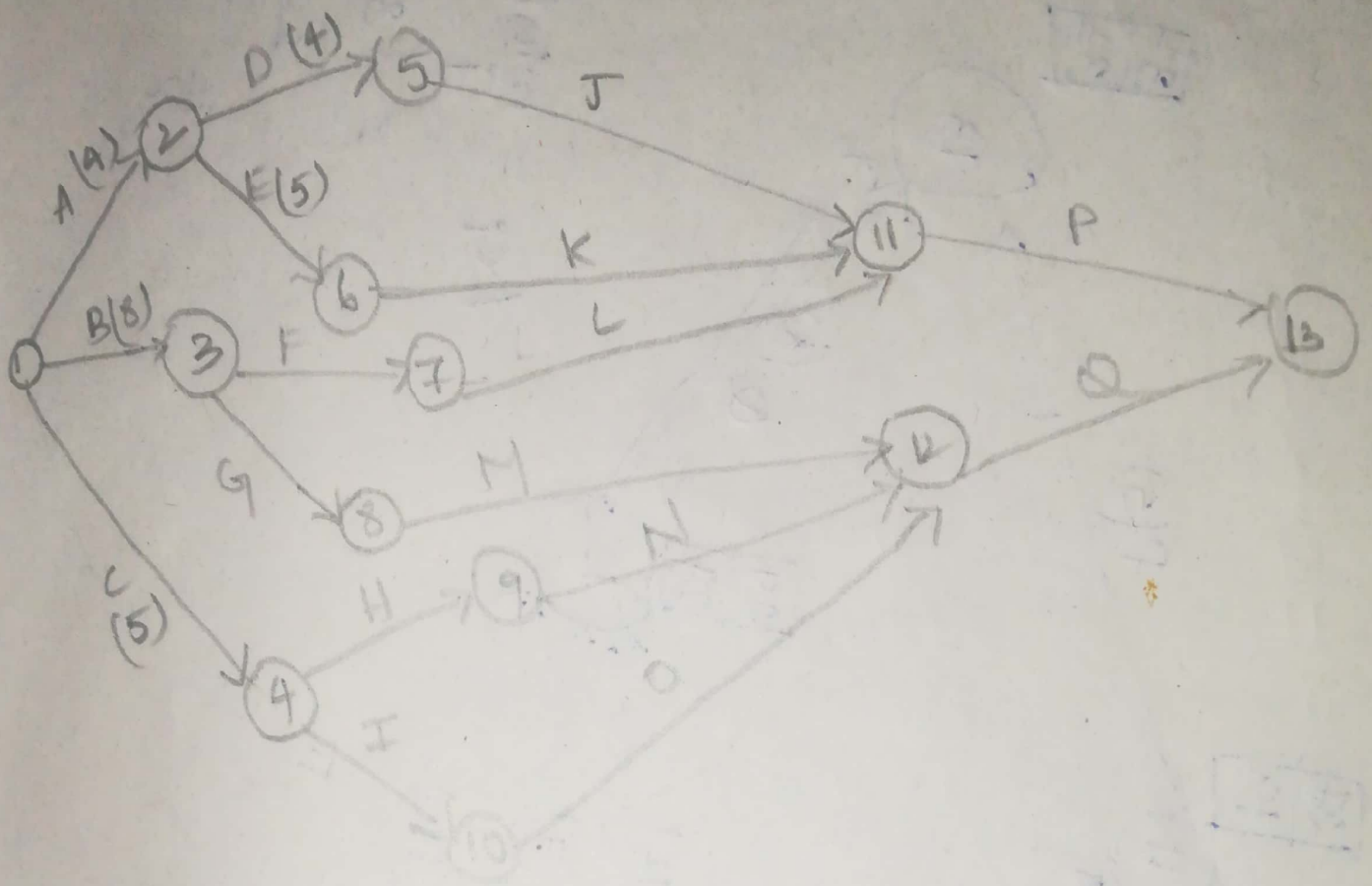
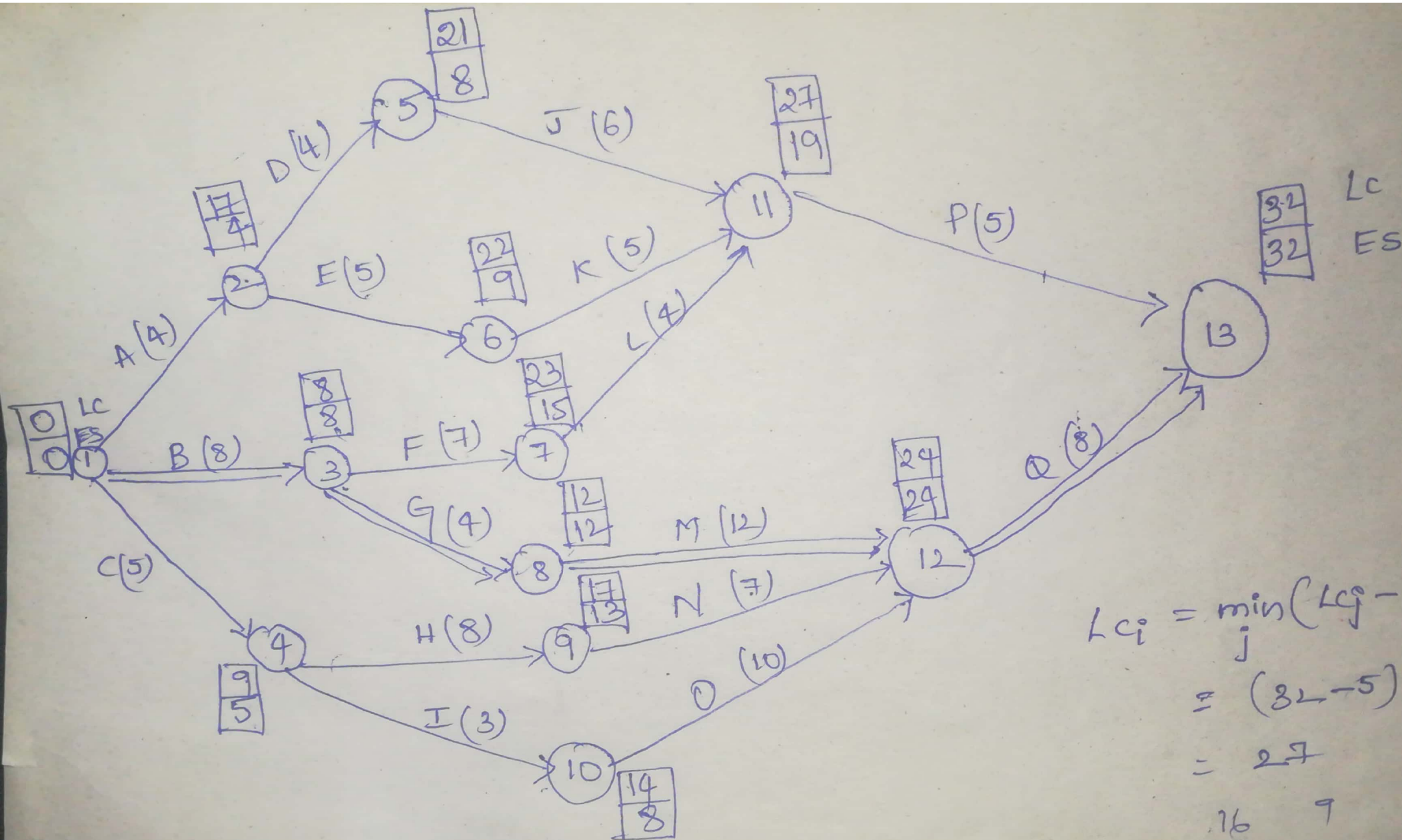


Consider the details of a project

Activity	Immediate predecessor(s)	Duration (Months)
A	—	4
B	—	8
C	—	5
D	A	4
E	A	5
F	B	7
G	B	4
H	C	8
I	C	3
J	D	6
K	E	5
L	F	4
M	G	12
N	H	7
O	I	10
P	J, K, L	5
Q	M, N, O	8

- find out construct the cpm network
- Determine the critical path.
- Compute total floats and free floats for non-critical activities





$$\begin{aligned}
 LC_i &= \min_j (LC_j - D_{ij}) \\
 &= (32 - 5) \\
 &= 27 \\
 &\quad \begin{array}{r} 16 \\ 8 \end{array} \quad 9
 \end{aligned}$$

32
24

b) critical path : 1-3-8-12-13
 B-G-M-Q = $8+4+12+8 = 32$

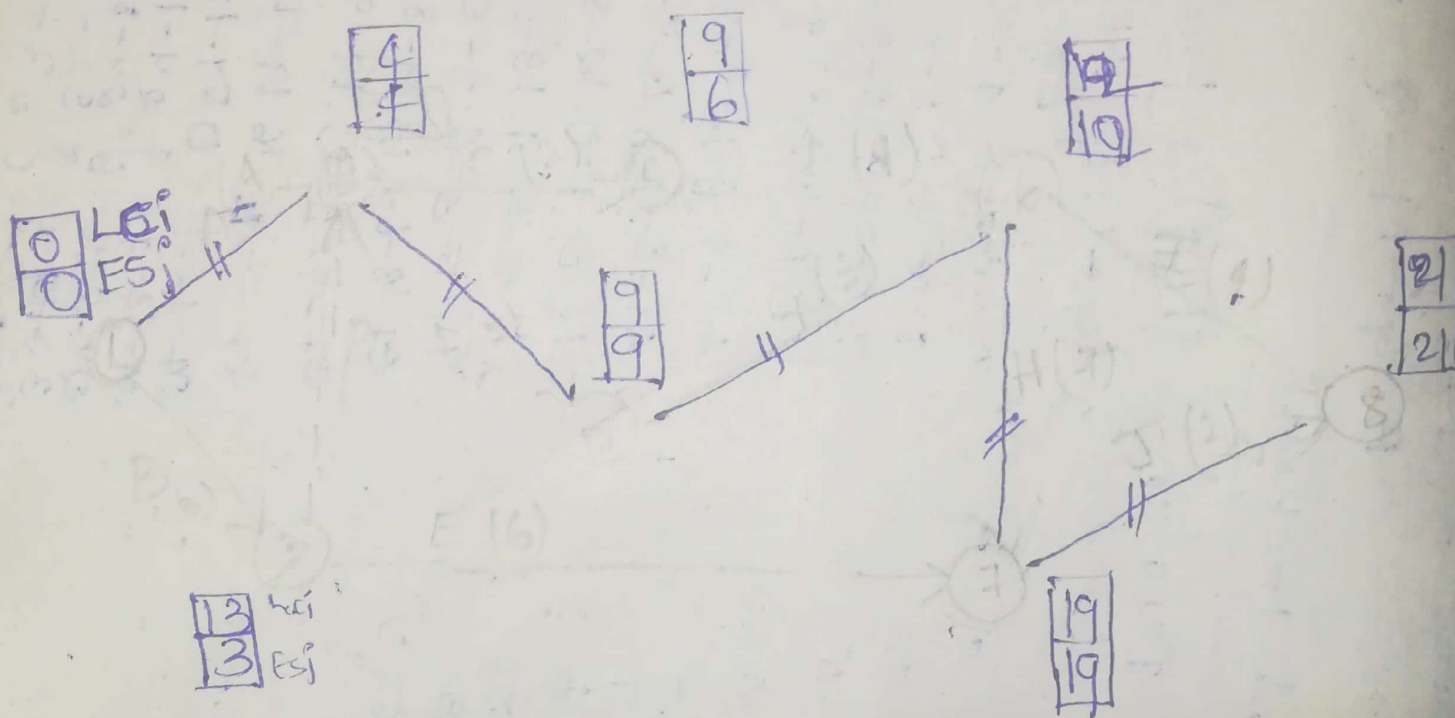
c) Total float and free float:

Activity	Duration	(TF) $LS_i - ES_i$	Free float (FF) $ES_j - ES_i - D_{ij}$
A 1-2	4	$17 - 0 - 4 = 13$	$4 - 0 - 4 = 0$
ⓑ 1-3	8	$8 - 0 - 8 = 0$	$8 - 0 - 8 = 0$
Ⓒ 1-4	5	$9 - 0 - 5 = 4$	$5 - 0 - 5 = 0$
D 2-5	4	$21 - 4 - 4 = 13$	$8 - 4 - 4 = 0$
E 2-6	5	$22 - 4 - 5 = 13$	$9 - 4 - 5 = 0$
F 3-7	7	$23 - 8 - 7 = 8$	$15 - 8 - 7 = 0$
Ⓓ 3-8	4	$12 - 8 - 4 = 0$	$12 - 8 - 4 = 0$
Ⓔ 4-9	8	$17 - 5 - 8 = 4$	$13 - 5 - 8 = 0$
Ⓕ 4-10	3	$8 - 5 - 3 = 0$	$8 - 5 - 3 = 0$
Ⓖ 5-11	6	$14 - 5 - 3 = 6$	$19 - 8 - 6 = 5$
Ⓙ 6-11	5	$21 - 8 - 6 = 13$	$19 - 8 - 6 = 5$
Ⓚ 6-11	5	$27 - 9 - 5 = 13$	$19 - 9 - 5 = 5$
Ⓛ 7-11	4	$27 - 9 - 5 = 13$	$19 - 9 - 5 = 5$
Ⓜ 8-12	4	$19 - 15 - 4 = 0$	$19 - 15 - 4 = 0$
Ⓝ 8-12	12	$27 - 15 - 4 = 16$	$19 - 15 - 4 = 0$
Ⓟ 7-12	7	$27 - 15 - 4 = 16$	$19 - 15 - 4 = 0$
Ⓡ 10-12	10	$27 - 15 - 4 = 16$	$19 - 15 - 4 = 0$
Ⓢ 11-13	5	$24 - 12 - 12 = 0$	$24 - 12 - 12 = 0$
Ⓣ 11-13	5	$24 - 13 - 7 = 4$	$24 - 13 - 7 = 4$
Ⓤ 12-13	8	$24 - 8 - 10 = 6$	$24 - 8 - 10 = 6$
Ⓡ 12-13	8	$32 - 19 - 5 = 8$	$32 - 19 - 5 = 8$
Ⓡ 12-13	8	$32 - 24 - 8 = 0$	$32 - 24 - 8 = 0$

CPM - (2) problem

21
12

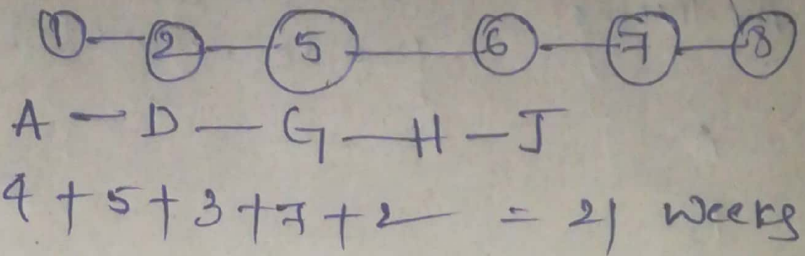
Activity	immediate predecessor(s)	Duration (week)
A	—	4
B	—	3
C	A, B	2
D	A, B	5
E	B	6
F	C	4
G	D	3
H	F, G	7
I	F, G	4
J	E, H	2



$$ES_j = \left(ES_i + D_{ij} \right) \text{ Max.}$$

$$LC_i = \text{Min} \left(LC_j + D_{ij} \right)$$

critical path:

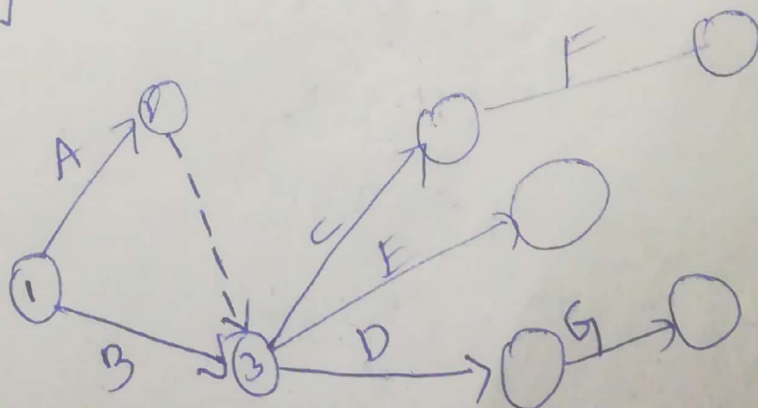


Non-critical Activity	free float (week) $ES_j - ES_i - D_{ij}$	total float (week) $LS_j - ES_i - D_{ij}$
1-3 B	3 - 3 - 0 - 3 = 0	13 - 0 - 3 = 10
2-4 C	9 - 4 - 2 = 2	9 - 4 - 2 = 3
3-7 E	19 - 13 - 6 = 0	19 - 13 - 6 = 0
4-6 F	12 - 6 - 4 = 2	12 - 6 - 4 = 2
6-7 H	19 - 12 - 7 = 0	
6-8 I	21 - 12 - 4 = 5	21 - 12 - 4 = 5

$\frac{24}{16}$

$$LS_j - ES_i - D_{ij} = 13 - 0 - 3 = 10$$

$$ES_j - ES_i - D_{ij} = 3 - 0 - 3 = 0$$



Activity	immediate predecessors (s)	Duration (Months)
A	—	5
B	—	2
C	—	3
D	A	4
E	C	2
F	B	4
G	D	7
H	E, F	6

$$\left(\frac{9-1}{6}\right)^2 = \left(\frac{8}{6}\right)^2 = \frac{64}{9}$$

$$\sigma^2 = \left(\frac{4}{3}\right)^2$$

$$\sigma = \sqrt{\frac{16}{9}} = \frac{4}{3}$$

A	—	$\frac{a+4m+b}{6} = \frac{3+20+8}{6} = 24.3$
B	—	$\frac{6+28+9}{6} = 35.5$
C	—	$\frac{4+20+9}{6} = 25.5$
D	—	$\frac{3+20+8}{6} = 24.3$
E	—	$\frac{4+24+9}{6} = 29.5$
F	—	$\frac{5+32+11}{6} = 38.8$
G	—	$\frac{3+24+9}{6} = 28.5$
H	—	$\frac{1+8+9}{6} = 3$ / 209.4

activity.
consider

the following data of a project

Activity

predecessor(s)

Duration(week)

a	m	b
3	5	8
6	7	9
4	5	9
3	5	8
4	6	9
5	8	11
3	6	9
1	2	9

A

—

B

—

C

A

D

B

E

A

F

C, D

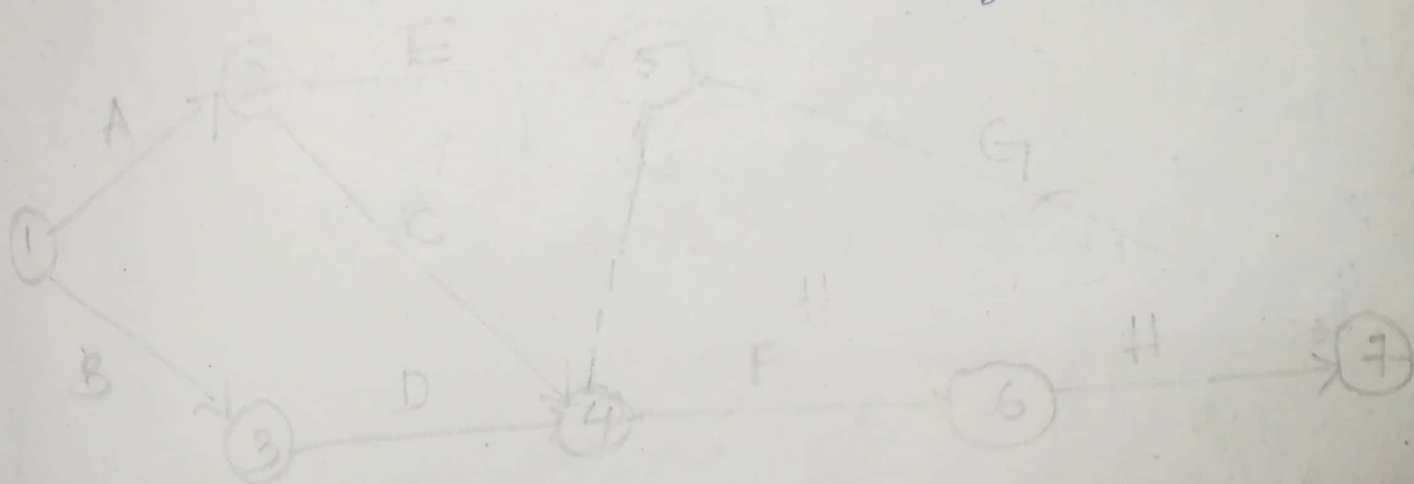
G

C, D, E

H

F

$3+2+8$



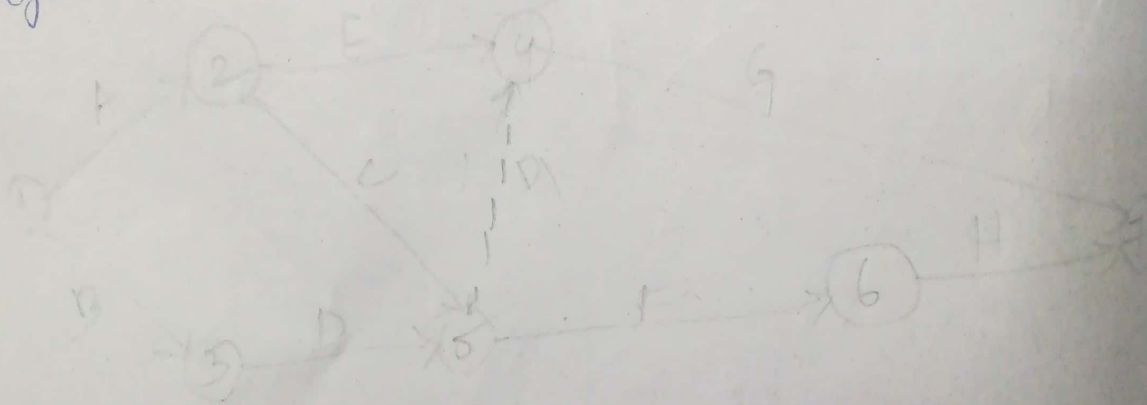
PERT

Consider the following data of a project.

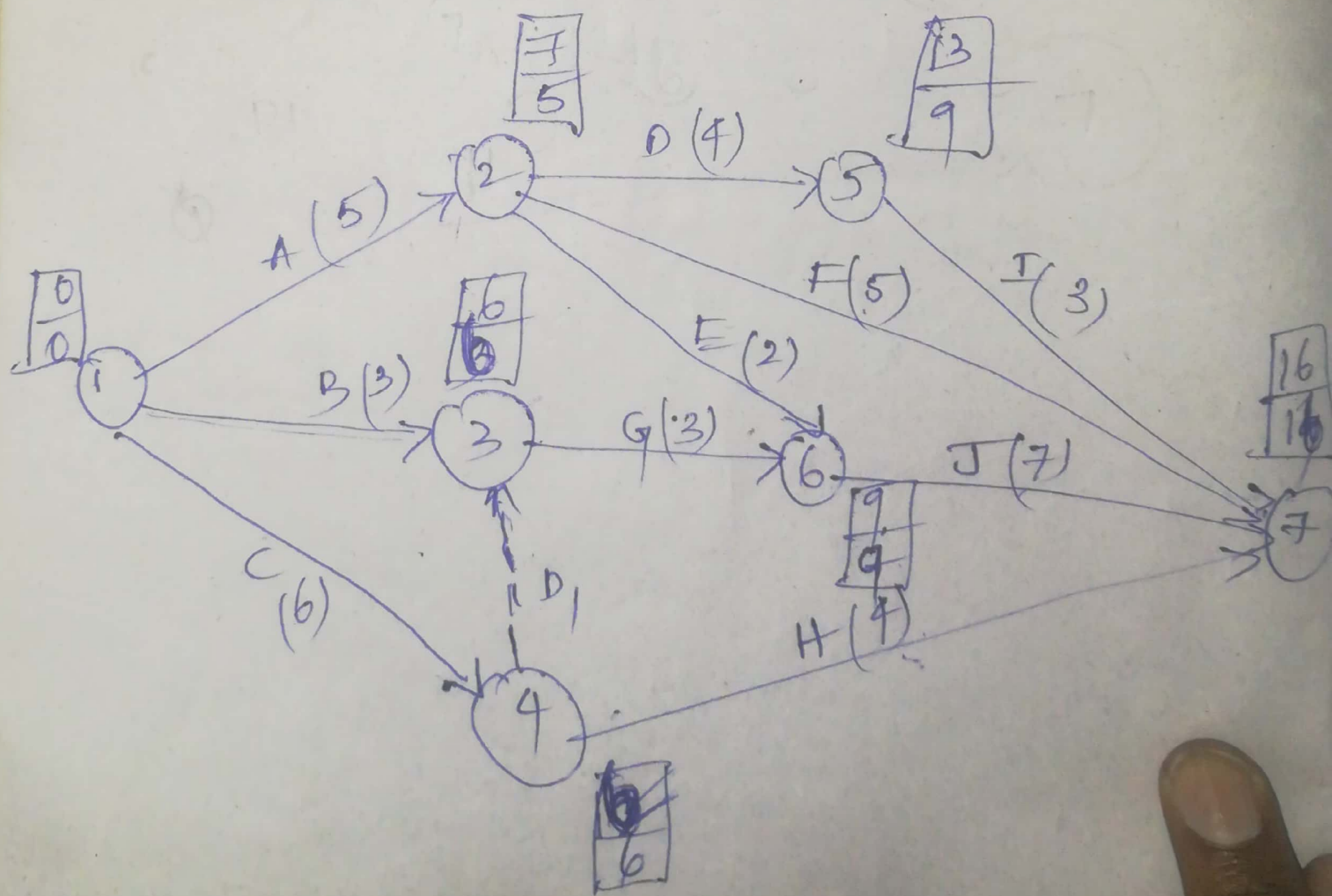
Activity	predecessor(s)	Duration (weeks)		
		a	m	b
A	—	3	5	8
B	—	6	7	9
C	A	4	5	9
D	B	3	5	8
E	A	4	6	9
F	C, D	5	8	11
G	C, D, E	3	6	9
H	F	1	2	7

Mean
at
 $\frac{3+20+8}{6}$

- Construct project Network?
- find the expected duration and variance of each activity.
- find the critical path and the expected project completion time.
- what is probability of completing the project on or before 30 weeks?
- If the probability of completing the project is 0.9 find the



Activity	Immediate predecessors	Duration			Mean $\mu = \frac{a+4m+b}{6}$	Variance $\sigma^2 = \left(\frac{b-a}{6}\right)^2$
A	—	4	4	10	5	1.00
B	—	1	2	9	3	1.78
C	—	2	5	14	6	4.00
D	A	1	4	7	4	1.00
E	A	1	2	3	5	0.11
F	A	1	5	9	3	1.78
G	B, C	1	2	4	4	0.00
H	C	4	4	8	8	1.00
I	D	6	7	8	7	0.11
J	E, G					



C.P. ~~1-4-6-7~~ 1-4-6-7
 C-D-1-6-5 ~~1-4-6-7~~ = ~~3+3+4~~

1-4, -3-6-7

Expected projected completion time is 16 weeks

$$P(x \leq c) = \left(\frac{x - \mu}{\sigma} \leq \frac{c - \mu}{\sigma} \right)$$

$$P(x \leq 35) = \left(z \leq \frac{c - \mu}{\sigma} \right)$$

$$= \left(z \leq \frac{35 - 16}{5.89} \right)$$

$$= (z \leq 7.82)$$

$$= (z \leq$$

Sum of all var
 critical activity

$$\sigma = \sqrt{5.89} \text{ weeks}$$

$$\sigma = 2.42$$

Sum of variance of critical activity =

$$\sigma^2 = 4 + 1.78 + 0.11 = 5.89$$

$$\sigma = \sqrt{5.89} = 2.42$$

$$= \left(z \leq \frac{35 - 16}{2.42} \right)$$

$$P(x \leq 35) = (z \leq 7.851)$$

$$= 0.99$$

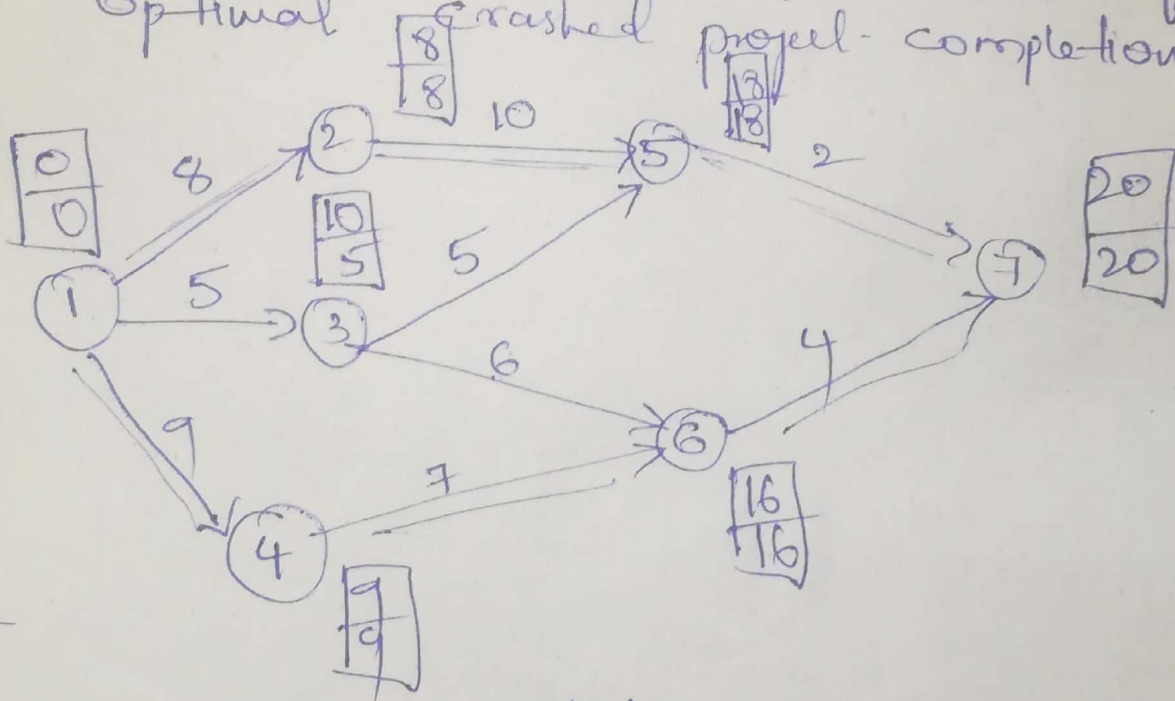
A project composed of 7 activities whose time estimates are as follows.

Activity	time in week			mean	varian.
	t_o	t_m	t_p		
1-2	1	1	7		
1-3	1	4	7		
1-4	2	4	18		
2-5	1	1	1		
3-5	2	5	14		
4-6	2	5	8		
5-6	3	6	15		

- i) Draw PERT N-D
- ii) Calculate slack of each event?
- iii) Identify critical path.
- iv) find the duration of project.

Activity	Normal time (t_n)	Normal cost (C_n) Rs	Crash time (t_c) weeks	Crash Cost (Rs)	Slope $\frac{C_c - C_n}{t_n - t_c}$
1-2	8	800	5	950	$\frac{150}{3} = 50$
1-3	5	500	3	700	$\frac{200}{2} = 100$
1-4	9	600	6	1050	$\frac{450}{3} = 150$
2-5	10	900	8	1300	$\frac{400}{2} = 200$
3-5	5	700	3	1100	$\frac{400}{2} = 200$
3-6	6	1200	5	1500	$\frac{300}{1} = 300$
4-6	7	1300	5	1400	$\frac{100}{2} = 50$
5-7	2	400	1	500	$\frac{100}{1} = 100$
6-7	4	500	2	900	$\frac{400}{2} = 200$

If the indirect cost/week is Rs. 300 find the optimal crashed project completion time.



project complete = 20 weeks

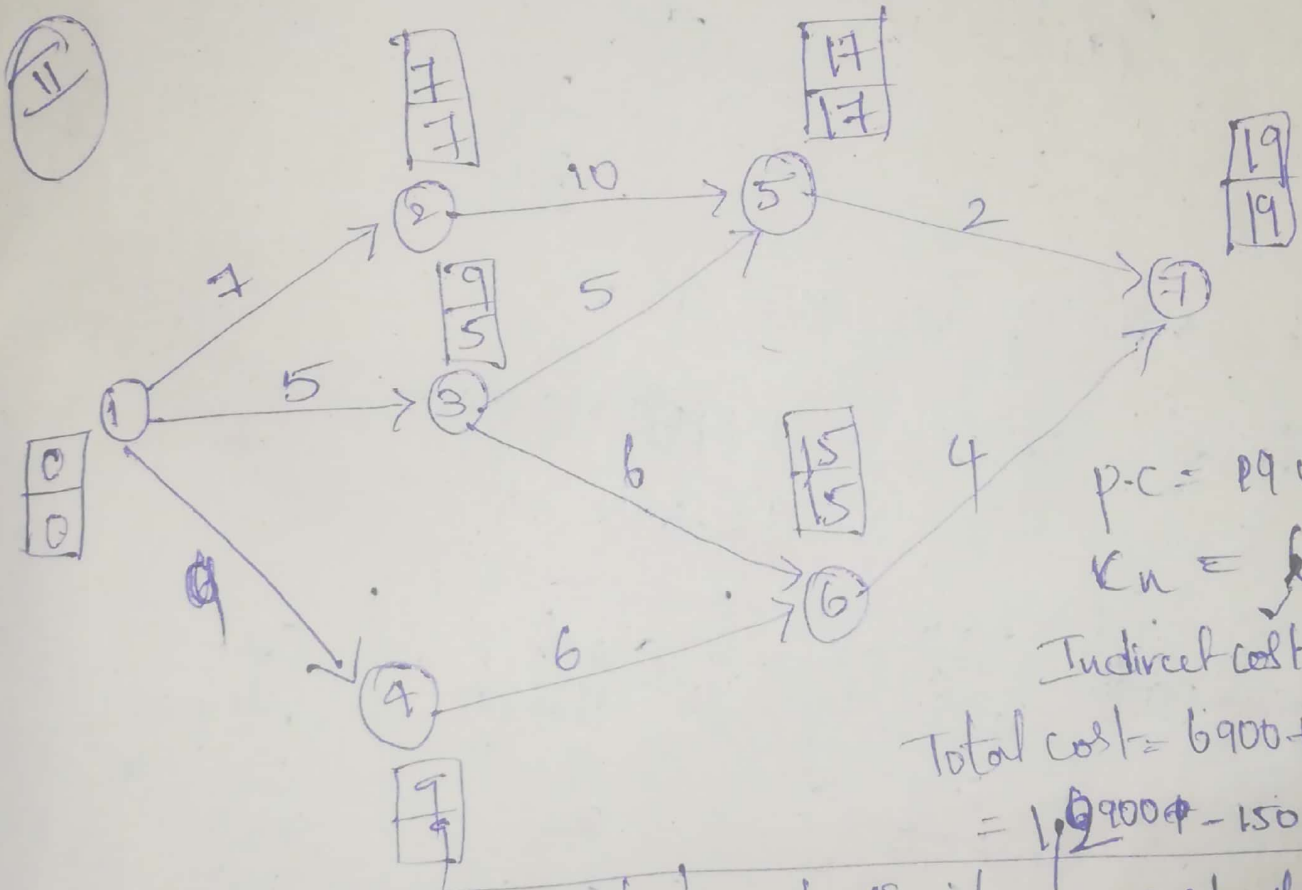
Normal cost = Rs 6,900

Indirect cost = $20 \times 300 = 6000$

Total cost = Rs. 12,900

critical path	Critical Activity	crash limit $t_n - t_c$	cost slope
1-2-5-7	1-2	3 2	50 *
	2-5	2	200
	5-7	1	100
1-4-6-7	1-4	6	150
	4-6	5 4	100 *
	6-7	2	200

12900
1200

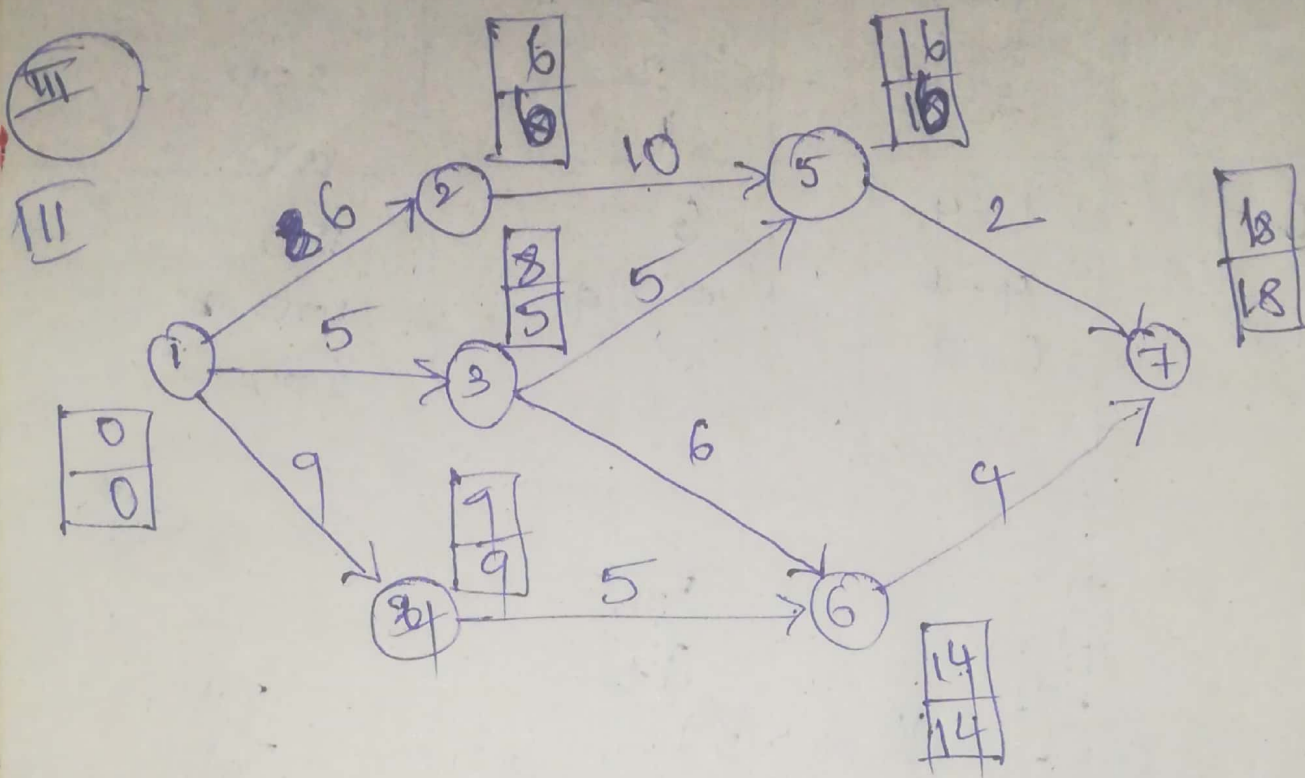


p.c = 19 weeks
 $K_n = 6900$
 Indirect cost = 6000
 Total cost = $6900 + (50 \times 100)$
 $= 12900 - 150 = 12750$

Critical path	Critical Activity	crash limit	cost slope.
1-2-5-7	1-2	2 1	50 *
	2-5	2	200
	5-7	1	100
1-4-6-7	1-4	6	150
	4-6	4 3	100 *
	6-7	2	200

$$\text{Total cost} = 12900 + 150 - 300$$

$$= 13050 - 300 = 12750/-$$



Total no. of weeks = 18 w

$$\text{Total cost} = 12750 + 150 - 300$$

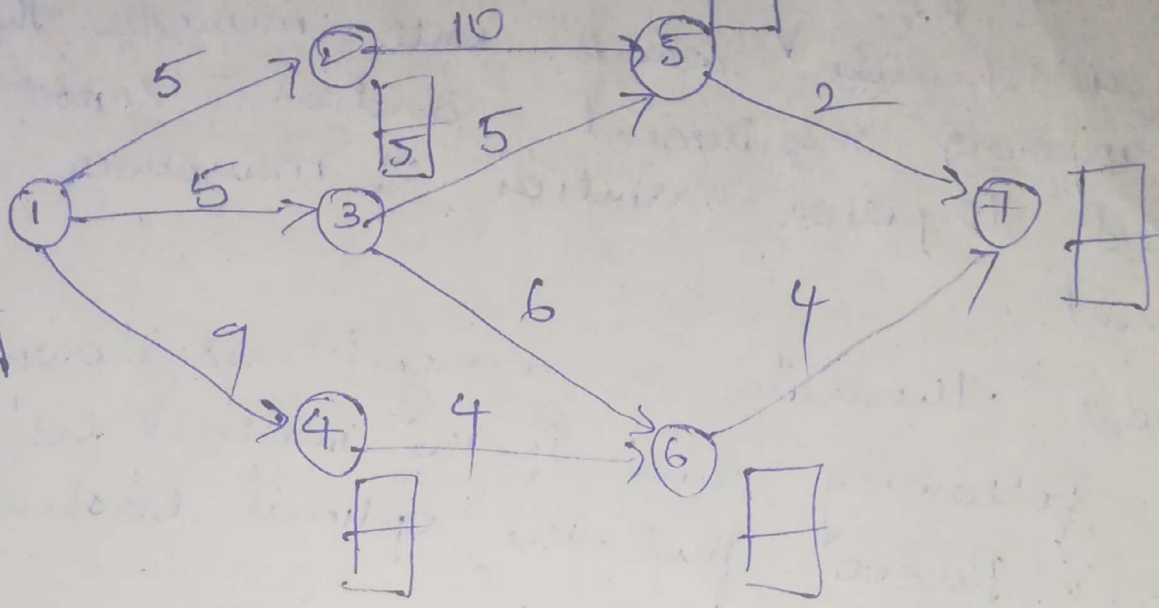
$$= 12600$$

Critical path	Critical activity	Crash limit	Cost slope
1-2-5-7	1-2	0	50 *
	2-5	2	200
	5-7	1	100
1-4-6-7	1-4	6	150
	4-6	2	100 *
	6-7	2	200

2

5

0
0

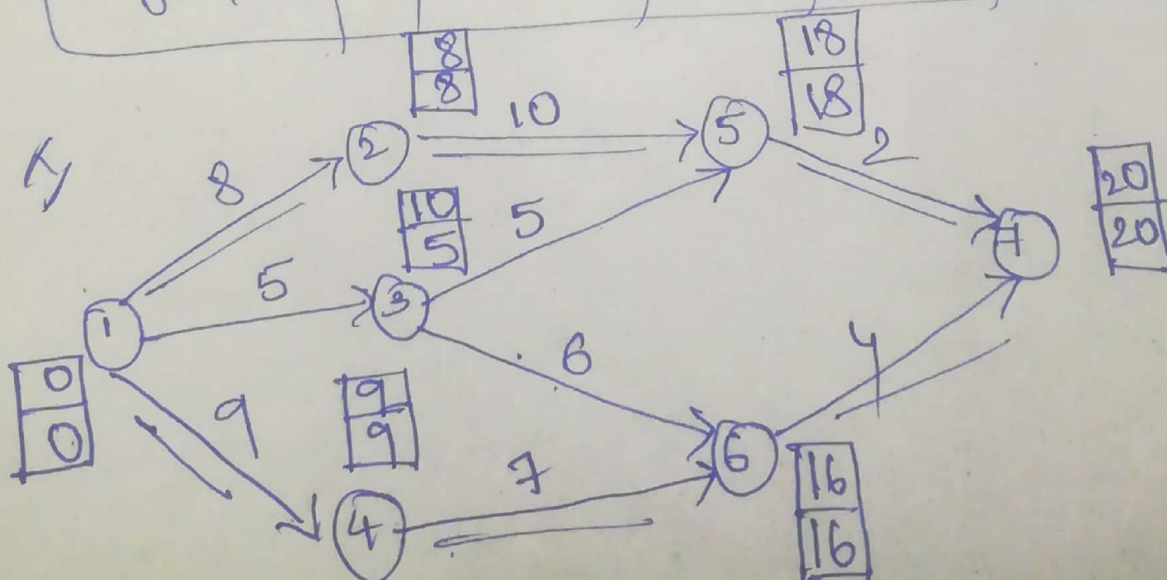


Crashing of Network

Considers the following problem of project scheduling
obtain a schedule which will minimize the
peak manpower requirement and also smooth
out period to period variation of manpower
requirement.

Consider the data of a project as shown
in the following data if the indirect cost
per week is Rs. 300 find the optimal crashed
project completion time.

Activity	Normal time (weeks) t_n	Normal cost C_n (₹)	Crash time (weeks) t_c	Crash cost C_c	slope (₹) $\frac{C_c - C_n}{t_n - t_c}$
1-2	8	800	5	950	50
1-3	5	500	3	700	100
1-4	9	600	6	1050	150
2-5	10	900	8	300	200
3-5	5	700	3	1100	200
3-6	6	1200	5	1500	300
4-6	7	1300	5	1400	100
5-7	2	400	1	500	100
6-7	4	500	2	900	200



The normal project completion time = 20 weeks

Critical path = 1-2-5-7

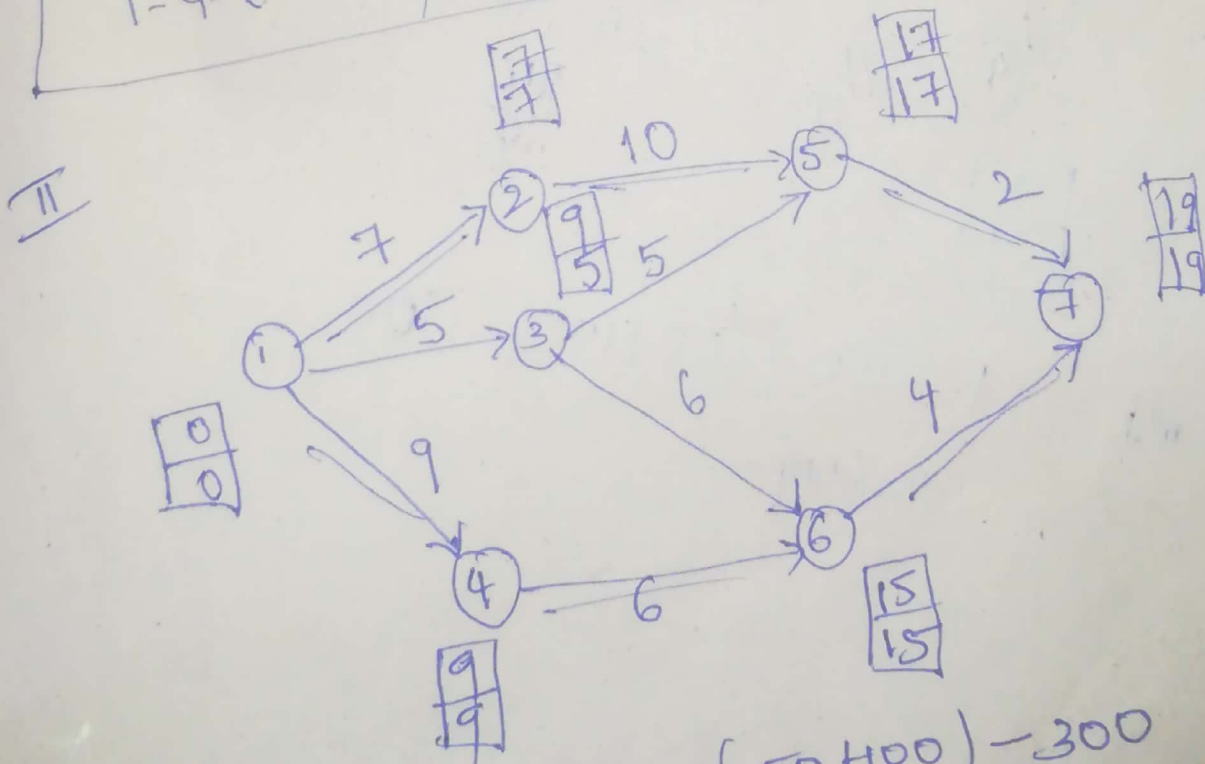
1-4-6-7

Total normal cost = 6900

Indirect cost = $(20 \times 300) = 6000$

total cost = 12900

Crash limit and slope		Crash limit cost slope	
Critical activity path	Critical activity	Crash limit	cost slope
1-2-5-7	1-2	3 2	50 *
	2-5	2	200
	5-7	1	100
1-4-6-7	1-4	3 2	150
	4-6	2 1	100 *
	6-7	2	200

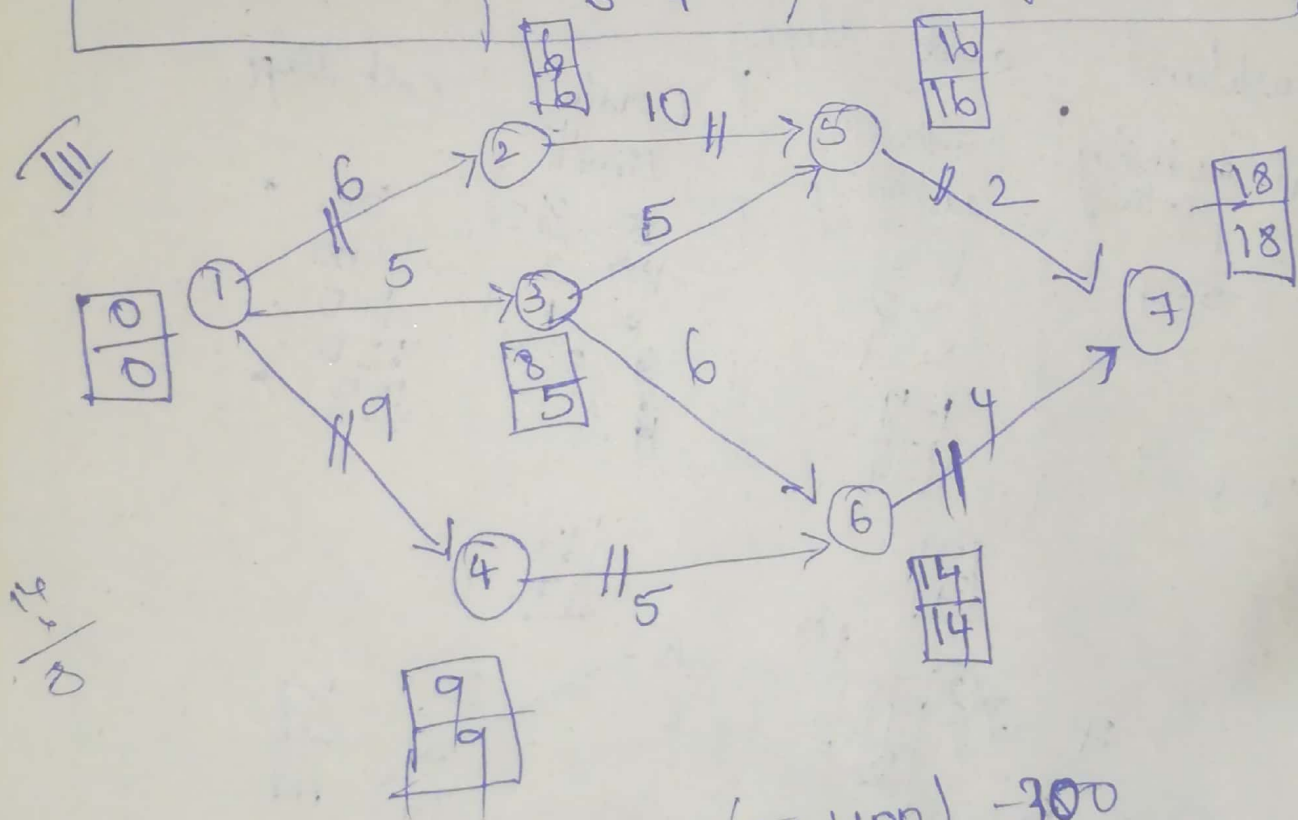


Total cost = $12,900 + (50 + 100) - 300$

= $12,900 + 150 - 300$

= 12,750/-

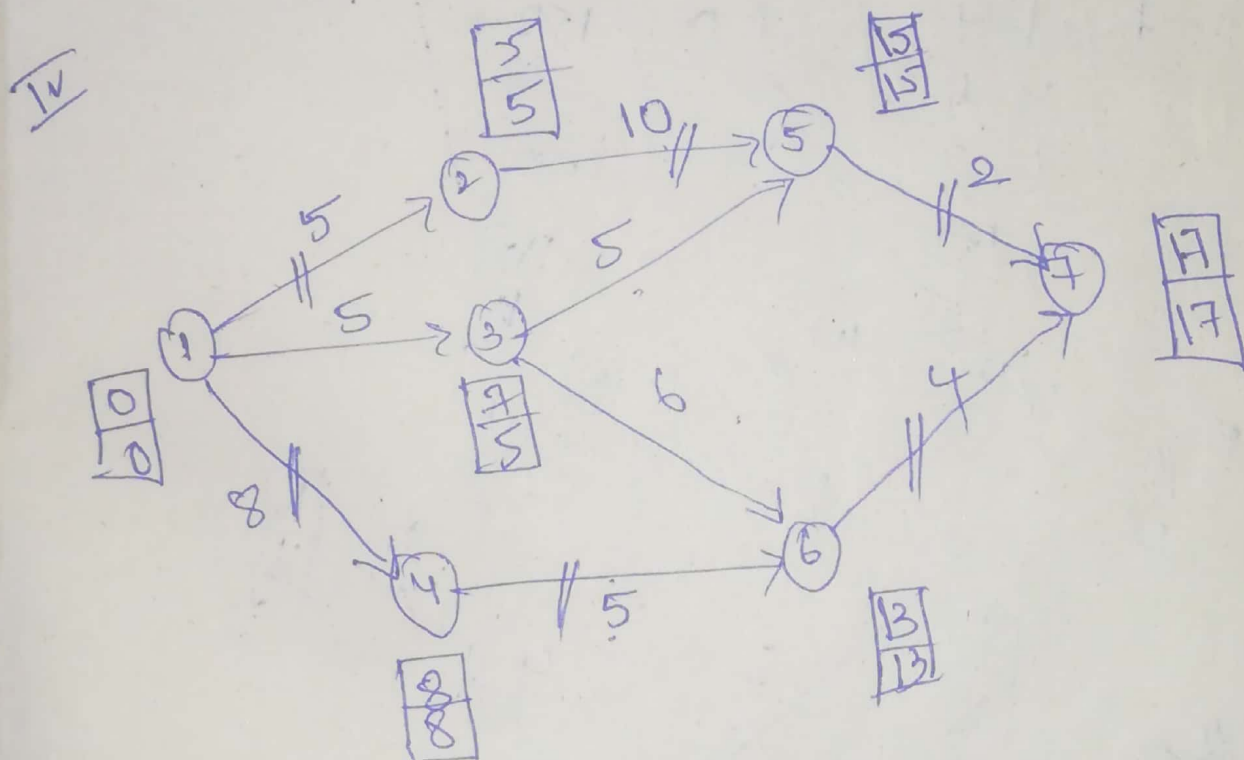
Critical Activity	Critical path	Crash limit	Cost slope
1-2-5-7	1-2	2	50*
	2-5	2	200
	5-7	1	100
1-4-6-7	1-4	2	150
	4-6	0	100*
	6-7	2	200



$$\text{Total cost} = 12,750 + (50 + 100) - 300$$

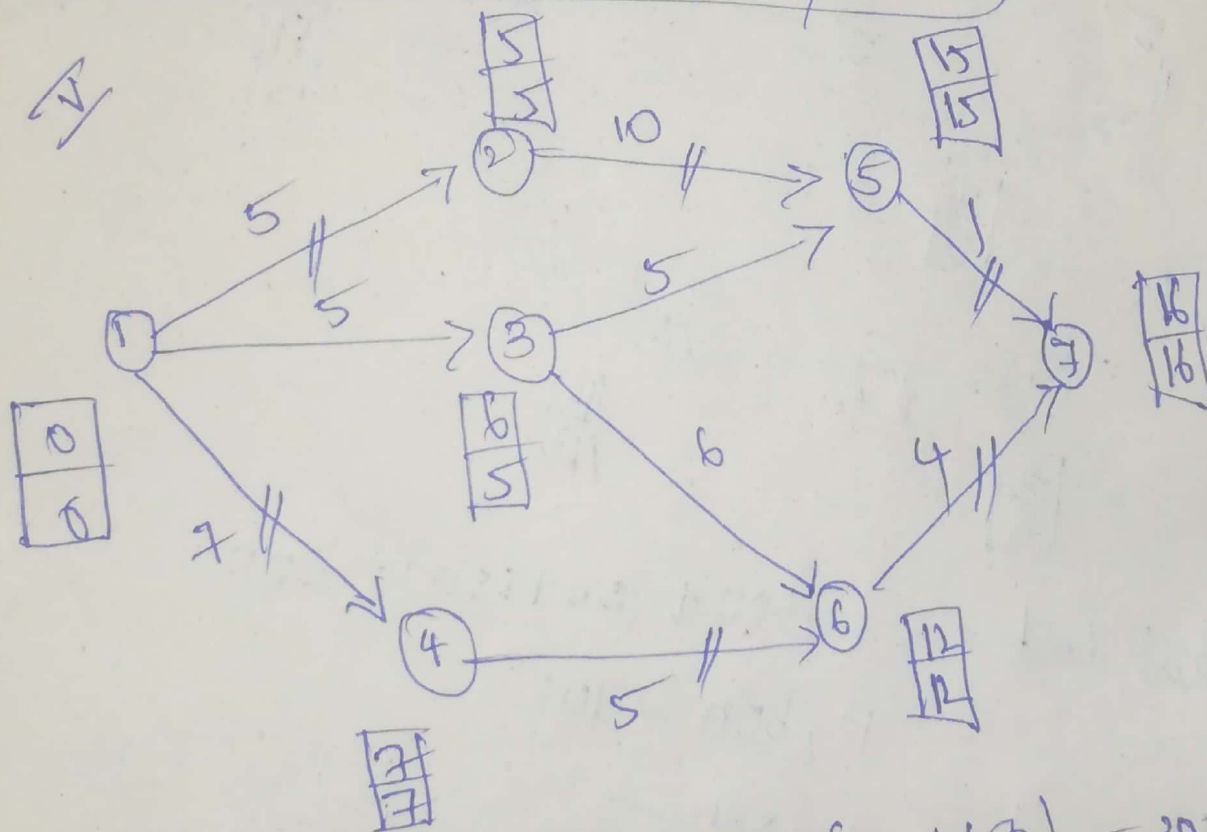
$$= 12,600/-$$

Critical Activity	Critical path	crash limit	Cost slope
1-2-5-7	1-2	0	50 *
	2-5	2	200
	5-7	1	100
1-4-6-7	1-4	1	150 *
	4-6	0	—
	6-7	2	200



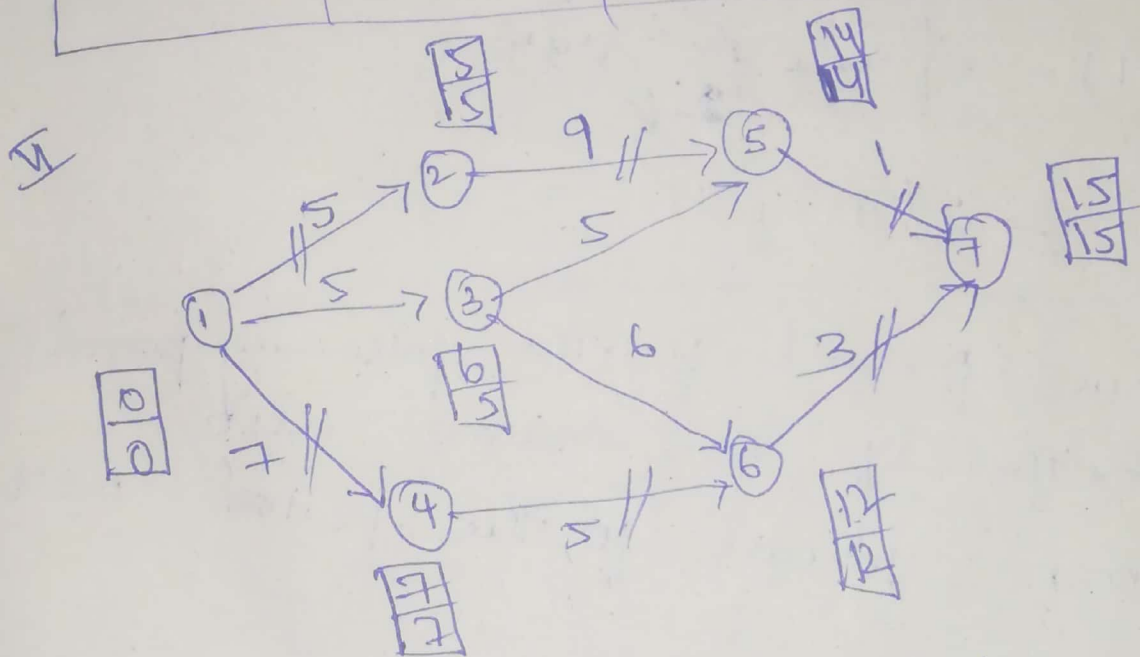
$$\begin{aligned}
 \text{Total cost} &= 14,600 + (50 + 150) - 300 \\
 &= 12,600 - 100 \\
 &= 12,500/-
 \end{aligned}$$

Critical activity	Critical path	Crash limit	Cost slope
1-2-5-7	1-2	0	—
	2-5	2	200
	5-7	10	100 *
1-4-6-7	1-4	10	150 *
	4-6	0	—
	6-7	2	200



$$\begin{aligned}
 \text{Total cost} &= 12,500 + (100 + 150) - 300 \\
 &= 12,500 - 50 \\
 &= 12,450/-
 \end{aligned}$$

Critical activity	Critical path	Crash limit	cost slope
1-2-5-7	1-2	0	—
	2-5	2	200
	5-7	0	—
1-4-6-7	1-4	0	—
	4-6	0	—
	6-7	2	200



$$\begin{aligned}
 \text{Total cost} &= 12,450 + (200 + 200) - 300 \\
 &= 12,450 + 100 \\
 &= 12,550 \text{ —}
 \end{aligned}$$

final projection completion time is = 16 weeks

critical path

i) 1-2-5-7

ii) 1-4-6-7